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# Mass transfer coefficient and concentration boundary layer thickness for a dissolving NAPL pool in porous media

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### Abstract

Analytical expressions for the time invariant, average mass transfer coefficient and the concentration boundary layer thickness applicable to dissolving single-component nonaqueous phase liquid (NAPL) pools in two-dimensional, saturated, homogeneous and isotropic porous formations are derived. Good agreement between predicted and experimentally determined time invariant average mass transfer coefficients is observed.

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*Keywords:* NAPL pool dissolution; Mass transfer coefficient; Concentration boundary layer; Contaminant transport; Analytical solutions

## 1. Introduction

Subsurface formations are often contaminated by nonaqueous phase liquids (NAPLs) originating from leaking underground storage tanks, ruptured pipelines, surface spills, hazardous waste landfills, disposal sites, and leachates from recycled wastes [19]. When a NAPL spill infiltrates a subsurface formation through the vadose zone, a portion of it may be trapped and immobilized within the unsaturated porous formation in the form of blobs

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## Nomenclature

- C aqueous-phase concentration (solute mass/aqueous volume, M/L<sup>3</sup>)
- $C_{\rm b}$  background (free stream) aqueous-phase concentration (M/L<sup>3</sup>)
- $C_{\rm s}$  aqueous saturation concentration (solubility, M/L<sup>3</sup>)
- $D_x$  longitudinal hydrodynamic dispersion coefficient (L<sup>2</sup>/T)
- $D_z$  hydrodynamic dispersion coefficient in the vertical direction (L<sup>2</sup>/T)
- $\mathcal{D}$  molecular diffusion coefficient (L<sup>2</sup>/T)
- $\mathcal{D}_{e}$  effective molecular diffusion coefficient, equal to  $\mathcal{D}/\tau^{*}$  (L<sup>2</sup>/T)
- k time invariant local mass transfer coefficient (L/T)
- $k^*$  time invariant average mass transfer coefficient (L/T)
- $K_{\rm d}$  distribution coefficient (L<sup>3</sup>/M)
- $\ell_x$  pool length along the x direction (L)
- $U_x$  average interstitial fluid velocity (L/T)
- *x* spatial coordinate (L)
- y spatial coordinate (L)

## Greek symbols

$\delta_{\rm c}$	concentration boundary layer thickness (L)
θ	porosity (liquid volume/aquifer volume, $L^3/L^3$ )
λ	decay coefficient for the aqueous-phase concentration $(T^{-1})$
$\lambda^*$	decay coefficient for the concentration sorbed onto the solid matrix $(T^{-1})$
ξ	dummy integration variable
ρ	bulk density of the porous medium $(M/L^3)$
τ*	tortuosity factor ( $\geq 1$ )
	•

or ganglia. Upon reaching the water table, dense nonaqueous phase liquids (DNAPLs) with densities heavier than that of water (sinkers, e.g. organic leachates from recycled hazardous solid wastes), given that the pressure head at the capillary fringe is sufficiently large, continue to migrate downward leaving behind trapped ganglia until they encounter an impermeable layer, where a flat source zone or pool starts to form [30]. NAPLs with densities lower than that of water (floaters, e.g. petroleum products) as soon as they reach the saturated region, spread laterally and float on the water table in the form of a pool [29]. As groundwater flows past trapped ganglia or NAPL pools, a fraction of the NAPL dissolves in the aqueous phase and a plume of dissolved hydrocarbons is created.

The aqueous-phase concentrations of dissolved NAPLs in groundwater are primarily governed by interphase mass transfer processes that often are slow and rate-limited [25]. Furthermore, the dissolution of NAPL pools in porous media is fundamentally different from that of residual blobs [6]. NAPL pools have limited contact areas with respect to groundwater. If the same volume of a NAPL is present as ganglia and as pool, ganglia dissolution is expected to proceed at a faster rate, because of the larger surface area available for interphase mass transfer [29]. Consequently, NAPL pools often lead to long-lasting sources of groundwater contamination.

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Numerous studies have focused on the migration and dissolution of residual blobs [1,5, 16,18,33,34], as well as on the dissolution of NAPL pools [3,10,13,17,21,22,24,26,30–32]. Furthermore, several theoretically and experimentally derived mass transfer relationships for the dissolution of residual NAPL blobs [15,28] and NAPL pools [8,12,20,23] have been presented in the literature.

Mathematical models for contaminant transport originating from NAPL pool dissolution often assume that the dissolution process is instantaneous when mass transfer rates at the NAPL–water interface are much faster than the advective-dispersive transport of the dissolved NAPLs away from the interface, and employ average and time invariant mass transfer coefficients which are representative of the entire pool [6,14]. In this work, analytical relationships for the average mass transfer coefficient and the concentration boundary layer thickness applicable to dissolving NAPL pools in two-dimensional, homogeneous subsurface formations under steady-state conditions are derived.

#### 2. Mathematical formulation

The task of obtaining analytical expressions for mass transfer coefficients applicable to a dissolving NAPL pool in water saturated porous media is not trivial. However, for relatively simple cases of well-defined NAPL pool geometries under ideal conditions, analytical expressions for mass transfer coefficients can be derived. For example, consider a single-component NAPL pool that is denser than water and is formed on top of a low permeability layer within a two-dimensional, saturated, homogeneous and isotropic porous medium. The steady-state transport of the dissolving NAPL into the aqueous phase under uniform flow conditions is governed by

$$U_x \frac{\partial C(x,z)}{\partial x} = D_x \frac{\partial^2 C(x,z)}{\partial x^2} + D_z \frac{\partial^2 C(x,z)}{\partial z^2} - \lambda C(x,z) - \lambda^* \frac{\rho}{\theta} K_d C(x,z), \quad (1)$$

where C(x, z) is the aqueous-phase solute concentration, x, z the spatial coordinates in the longitudinal and vertical (perpendicular to the interface) directions, respectively,  $U_x$ the average interstitial fluid velocity,  $D_x$  and  $D_z$  are the longitudinal and vertical hydrodynamic dispersion coefficients, respectively,  $\lambda$  is the first-order decay coefficient of the aqueous-phase concentration,  $\lambda^*$  the first-order decay coefficient of the concentration sorbed onto the solid matrix,  $\rho$  the bulk density of the solid matrix,  $\theta$  the porosity of the porous medium, and  $K_d$  is the partition or distribution coefficient.

For mathematical simplicity, it is hypothesized that the sorption of the dissolved NAPL can be described by a linear equilibrium isotherm and that the local chemical equilibrium assumption is valid. Furthermore, the last two terms on the right-hand side of the governing Eq. (1) account for decay due to possible biological/chemical degradation of the aqueous-phase concentration and the concentration sorbed onto the solid matrix. Although the direct inter-relationship between sorption of halogenated compounds onto solids and biotransformation has yet to be thoroughly examined, experimental evidence suggests that organic solutes undergo degradation primarily in the aqueous phase [2,27]. Therefore, in order to make the present model general, two different decay coefficients are employed.



Fig. 1. Schematic illustration of the conceptual model showing a NAPL pool with length  $\ell_x$  within a porous formation under unidirectional interstitial velocity  $U_x$ . The concentration within the boundary layer decreases from saturation concentration,  $C_s$ , at the NAPL–water interface to background concentration,  $C_b$ , in the bulk interstitial liquid.

To further simplify the physical system we assume that advective transport is much greater than the corresponding dispersive transport along the *x* direction ( $U_x \gg D_x$ ). For this limiting case the governing Eq. (1) reduces to

$$U_x \frac{\partial C(x,z)}{\partial x} = D_z \frac{\partial^2 C(x,z)}{\partial z^2} - \lambda C(x,z) - \lambda^* \frac{\rho}{\theta} K_{\rm d} C(x,z).$$
(2)

For the system examined here, as illustrated in Fig. 1, the appropriate initial and boundary conditions are:

$$C(0, z) = 0,$$
 (3)

$$C(x,0) = C_s,\tag{4}$$

$$C(x,\infty) = 0,\tag{5}$$

where  $C_s$  is the aqueous saturation (solubility) concentration of the dissolved NAPL at the NAPL–water interface. The solution to (2) subject to conditions (3)–(5) is obtained by straightforward Laplace transform procedures to yield

$$C(x, z) = \frac{C_{s}}{2} \exp\left[\frac{z}{D_{z}^{1/2}} \left(\lambda + \lambda^{*} \frac{\rho}{\theta} K_{d}\right)^{1/2}\right]$$

$$\times \operatorname{erfc}\left\{\frac{z}{2} \left(\frac{U_{x}}{D_{z}x}\right)^{1/2} + \left[\frac{x}{U_{x}} \left(\lambda + \lambda^{*} \frac{\rho}{\theta} K_{d}\right)\right]^{1/2}\right\}$$

$$+ \frac{C_{s}}{2} \exp\left[-\frac{z}{D_{z}^{1/2}} \left(\lambda + \lambda^{*} \frac{\rho}{\theta} K_{d}\right)^{1/2}\right]$$

$$\times \operatorname{erfc}\left\{\frac{z}{2} \left(\frac{U_{x}}{D_{z}x}\right)^{1/2} - \left[\frac{x}{U_{x}} \left(\lambda + \lambda^{*} \frac{\rho}{\theta} K_{d}\right)\right]^{1/2}\right\},$$
(6)

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where  $erfc[\cdot]$  is the complementary error function defined as

$$\operatorname{erfc}[\eta] = 1 - \operatorname{erf}[\eta] = 1 - \frac{2}{\pi^{1/2}} \int_0^{\eta} \exp[-\xi^2] \,\mathrm{d}\xi, \tag{7}$$

erf[·] is the error function, and  $\xi$  is a dummy integration variable. The analytical solution (6) can be used to predict aqueous-phase concentrations resulting from NAPL pool dissolution in a two-dimensional aquifer at steady-state conditions. For the special case where the dissolved NAPL concentration is conservative the two first-order decay coefficients are equal to zero ( $\lambda = \lambda^* = 0$ ) and (6) reduces to the familiar expression:

$$C(x, z) = C_{\rm s} \operatorname{erfc}\left[\frac{z}{2} \left(\frac{U_x}{D_z x}\right)^{1/2}\right].$$
(8)

The preceding expression for the aqueous-phase concentration is independent of  $K_d$ , because at steady-state conditions the magnitude of  $K_d$  (or equivalently the retardation factor) does not affect the dissolved NAPL concentration in the homogeneous aquifer when  $\lambda = \lambda^* = 0$  [9].

#### 3. Time invariant average mass transfer coefficient

The mass flux from a NAPL–water interface into the aqueous interstitial fluid within a water saturated, two-dimensional, homogeneous porous formation is described by the following relationship [9]:

$$-\mathcal{D}_{e} \left. \frac{\partial C(x,z)}{\partial z} \right|_{z \to 0} = k(x) [C_{s} - C(x,\infty)], \tag{9}$$

where  $\mathcal{D}_{e} = \mathcal{D}/\tau^{*}$  is the effective molecular diffusion coefficient (where  $\mathcal{D}$  is the molecular diffusion coefficient, and  $\tau^{*} \geq 1$  is the tortuosity coefficient), and *k* is the time invariant local mass transfer coefficient. Conventionally, any location above the concentration boundary layer is considered as  $z \to \infty$ . For the case where the background concentration is constant with respect to time and space, for notational convenience,  $C(x, \infty)$  is replaced by  $C_{b}$ , the constant background aqueous-phase concentration. It should be noted that in this study the free stream concentration is assumed to be zero ( $C_{b} = 0$ ). The mass transfer relationship (9) implies that the dissolution at the NAPL–water interface is limited only by mass transfer. The concentration along the interface is assumed constant and equal to the saturation concentration,  $C(x, 0) = C_{s}$ . For a NAPL–water interfacial area with finite length, in view of (9), the appropriate expression for the time invariant average mass transfer coefficient is given by

$$k^* = -\frac{\mathcal{D}_{\rm e}}{\ell_x C_{\rm s}} \int_0^{\ell_x} \left. \frac{\partial C(\xi, z)}{\partial z} \right|_{z \to 0} \,\mathrm{d}\xi,\tag{10}$$

where  $\ell_x$  is the NAPL pool dimension in x direction as shown in Fig. 1.

Differentiating (6) with respect to z and taking the limit  $z \rightarrow 0$  yields

$$\frac{\partial C(x,z)}{\partial z}\Big|_{z\to 0} = -C_{\rm s} \left[\frac{1}{D_z} \left(\lambda + \lambda^* \frac{\rho}{\theta} K_{\rm d}\right)\right]^{1/2} \operatorname{erf} \left\{ \left[\frac{x}{U_x} \left(\lambda + \lambda^* \frac{\rho}{\theta} K_{\rm d}\right)\right]^{1/2} \right\} -C_{\rm s} \left(\frac{U_x}{\pi D_z x}\right)^{1/2} \exp\left[-\frac{x}{U_x} \left(\lambda + \lambda^* \frac{\rho}{\theta} K_{\rm d}\right)\right].$$
(11)



Fig. 2. Variation of the time invariant overall mass transfer coefficient as a function of (a) pool length, (b) interstitial velocity, (c) vertical hydrodynamic dispersion coefficient, and (d) overall decay coefficient (here  $\ell_x = 7.7$  cm,  $U_x = 1.5$  cm/h,  $D_z = 0.05$  cm<sup>2</sup>/h, and  $\lambda = \lambda^* = 0$  h<sup>-1</sup>).

Substituting (11) into (10) and integrating enables us to obtain the desired expression for the time invariant average mass transfer coefficient

$$k^{*} = \frac{\mathcal{D}_{e}}{\ell_{x}} \left[ \frac{U_{x}}{2D_{z}^{1/2}} \left( \lambda + \lambda^{*} \frac{\rho}{\theta} K_{d} \right)^{-1/2} + \frac{\ell_{x}}{D_{z}^{1/2}} \left( \lambda + \lambda^{*} \frac{\rho}{\theta} K_{d} \right)^{1/2} \right] \\ \times \operatorname{erf} \left\{ \left[ \frac{\ell_{x}}{U_{x}} \left( \lambda + \lambda^{*} \frac{\rho}{\theta} K_{d} \right) \right]^{1/2} \right\} + \left( \frac{\mathcal{D}_{e}^{2} U_{x}}{\pi D_{z} \ell_{x}} \right)^{1/2} \exp \left[ -\frac{\ell_{x}}{U_{x}} \left( \lambda + \lambda^{*} \frac{\rho}{\theta} K_{d} \right) \right].$$
(12)

For the special case where the aqueous-phase NAPL concentration is conservative both  $\lambda$  and  $\lambda^*$  are equal to zero, and the preceding expression for  $k^*$  is simplified to

$$k^* = 2\mathcal{D}_{\rm e} \left(\frac{U_x}{\pi D_z \ell_x}\right)^{1/2}.$$
(13)

The sensitivity of the time invariant average mass transfer coefficient to its various model parameters, as predicted by (12), is illustrated in Fig. 2. It is shown in Fig. 2a that  $k^*$  decreases exponentially with increasing NAPL pool length. This behavior is expected because  $k^*$  represents the integral of the local mass transfer coefficient over the entire NAPL–water interface. It should be noted that the local mass transfer coefficient decreases with distance from the front end of the NAPL pool and has a maximum value at the leading or upstream edge [7]. Fig. 2b indicates that  $k^*$  is proportional to the interstitial fluid velocity. This behavior is attributed to increasing concentration gradients at the NAPL–water interface with increasing  $U_x$ . Fig. 2c shows that  $k^*$  decreases exponentially with increasing  $D_z$ . Enhancing the vertical spreading of the aqueous-phase concentration yields to smoother concentration gradients at the NAPL–water interface and consequently to smaller  $k^*$ . Fig. 2d indicates that  $k^*$  is directly proportional to the overall decay coefficient which is defined here as  $\lambda + \lambda^* \rho(K_d/\theta)$ . Increasing the decay rate of the aqueous-phase and sorbed concentrations



Fig. 3. Comparison between experimentally determined (solid circles) and analytically predicted (solid curve) time invariant average mass transfer coefficients. The experimental data are adapted from [11].

leads to steeper concentration gradients at the NAPL–water interface and consequently to greater  $k^*$ .

A favorable comparison between available, experimentally determined time invariant average mass transfer coefficients for seven different interstitial velocities associated with the dissolution of a TCE pool in a water saturated bench-scale aquifer [10,11,23] and those predicted by (12) is presented in Fig. 3. Therefore, the analytical expression for  $k^*$  derived in this study may be useful for NAPL pool dissolution investigations where experimental data or pertinent mass transfer coefficient correlations are not available.

#### 4. Concentration boundary layer thickness

The concentration boundary layer thickness,  $\delta_c$ , is defined as the vertical distance from the NAPL–water interface where the aqueous-phase concentration *C* is 1% of the saturation concentration  $C_s$  ( $C = 0.01C_s$ ) [4]. For the case where  $\lambda = \lambda^* = 0$ ,  $z = \delta_c$  and  $C/C_s = 0.01$ , the analytical solution (6) can be written as

$$0.01 = \operatorname{erfc}\left[\frac{\delta_{c}}{2} \left(\frac{U_{x}}{D_{z}x}\right)^{1/2}\right] = 1 - \operatorname{erf}\left[\frac{\delta_{c}}{2} \left(\frac{U_{x}}{D_{z}x}\right)^{1/2}\right],\tag{14}$$

where the latter formulation is a consequence of (7). The preceding relationship is valid only when the argument of the error function is equal to

$$\frac{\delta_{\rm c}}{2} \left(\frac{U_x}{D_z x}\right)^{1/2} = 1.82 \approx 2. \tag{15}$$

Solving for  $\delta_c$  yields the following expression for the boundary layer thickness resulting from a conservative dissolving NAPL pool in a two-dimensional, homogeneous, water saturated porous formation

$$\delta_{\rm c} \approx 4 \left(\frac{D_z x}{U_x}\right)^{1/2}.\tag{16}$$

Although (16) is an approximate expression, it describes the relationship between the concentration boundary thickness and its associated parameters.

The behavior of  $\delta_c$  as a function of the various transport parameters is demonstrated graphically in Fig. 4. The concentration boundary layer grows steadily as the longitudinal distance from the source increases (Fig. 4a). This is attributed to the progressive dispersion of the dissolved concentration as it is carried by the moving interstitial fluid. A decrease in  $\delta_c$  is observed with increasing  $U_x$  (Fig. 4b). This is an intuitive result because increasing  $U_x$ leads to steeper concentration gradients at the NAPL–water interface. Finally,  $\delta_c$  is shown to increase with increasing  $D_z$  (Fig. 4c) due to the associated increase in vertical spreading of the aqueous-phase concentration. Furthermore, it is evident from Fig. 4 that under typical groundwater conditions  $\delta_c$  is just a few centimeters thick.



Fig. 4. Predicted concentration boundary layer as a function of (a) longitudinal distance from the source, (b) interstitial velocity, and (c) vertical hydrodynamic dispersion coefficient (here x = 7.7 cm,  $U_x = 1.5$  cm/h,  $D_z = 0.05$  cm<sup>2</sup>/h, and  $\lambda = \lambda^* = 0$  h<sup>-1</sup>).

## 5. Summary

Analytical expressions for the time invariant average mass transfer coefficient and for the concentration boundary layer thickness associated with the dissolution of a NAPL pool in two-dimensional porous media were derived. It was demonstrated that  $\delta_c$  increases with increasing x and  $D_z$ , and decreases with increasing  $U_x$ . The analytical expression for  $k^*$ (12) may be useful to NAPL pool dissolution studies where experimentally determined mass transfer coefficients are not available. The analytical expression for  $\delta_c$  (16) may be employed in experimental studies of NAPL pool dissolution where appropriate sampling locations for aqueous-phase concentration measurements are desired.

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